

# Positive Feedback and Relaxation Oscillators

## Lecture 2 – Relaxation Oscillators

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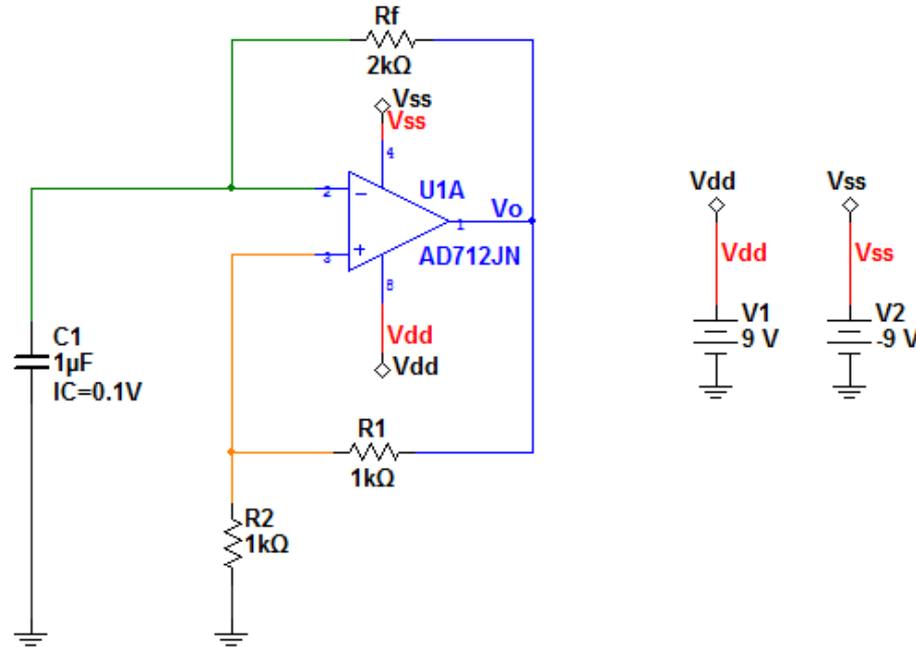
# Recall from last lecture...

1. The Schmitt Trigger
2. Instability in the physical Schmitt trigger – the parasitic capacitor

Questions?

# Goal of Lecture 2

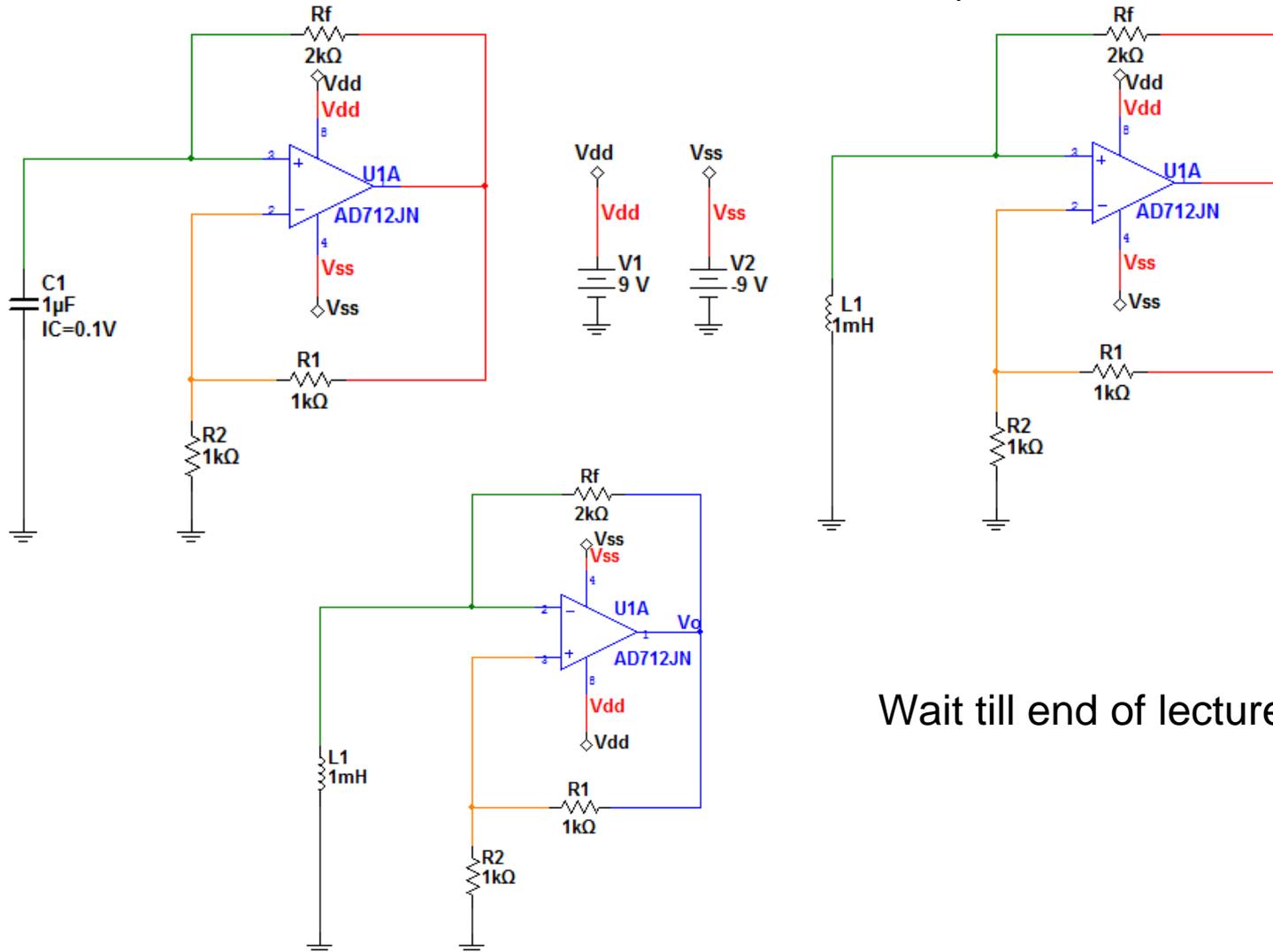
Analyze and simulate circuit shown below. Specifically, sketch  $V_o(t)$  in the circuit below. Note: You should realize circuit physically on a breadboard.



Recall : When you have questions, please ask!

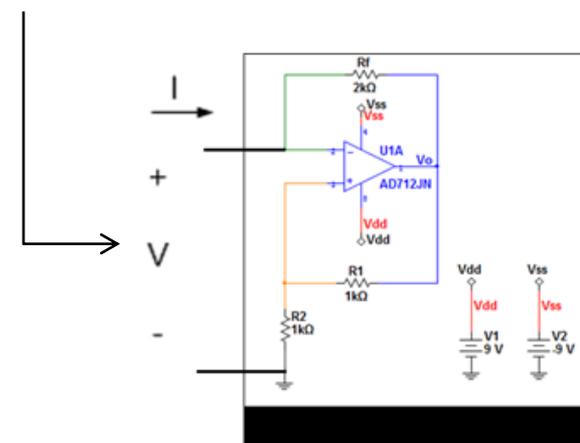
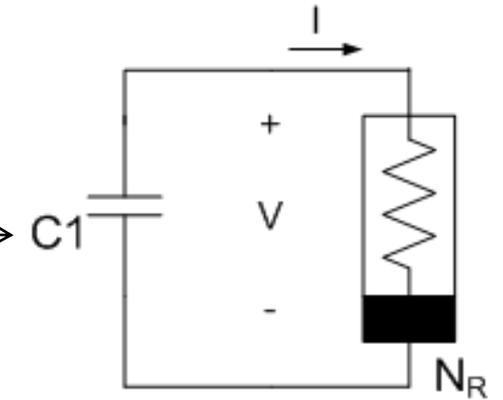
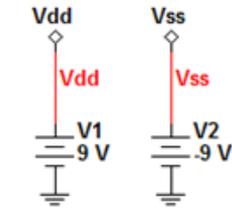
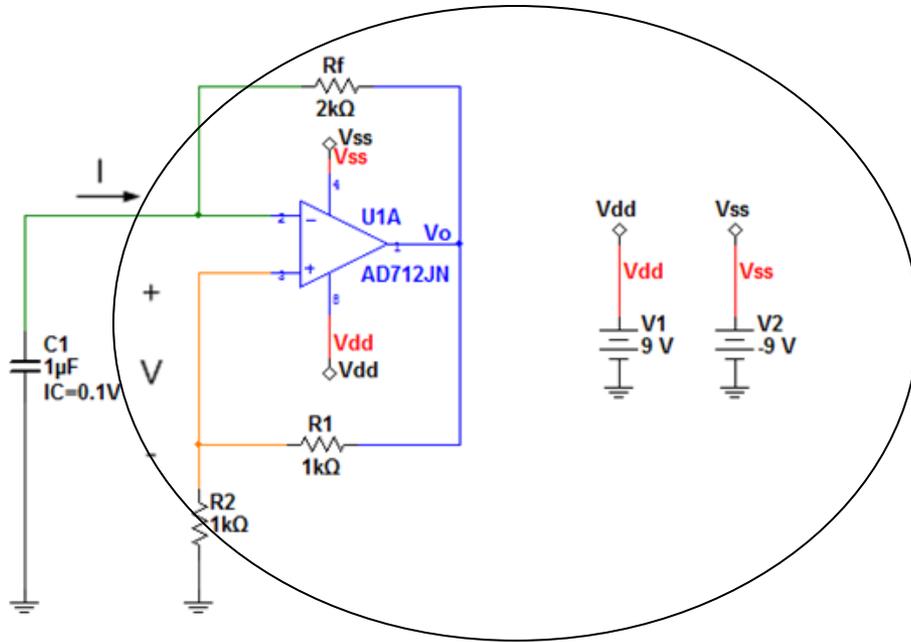
# If you have seen this circuit before...

What does each circuit below do (answer in ONE word)?



Wait till end of lecture 😊 ...

# Step 1: Understand Problem

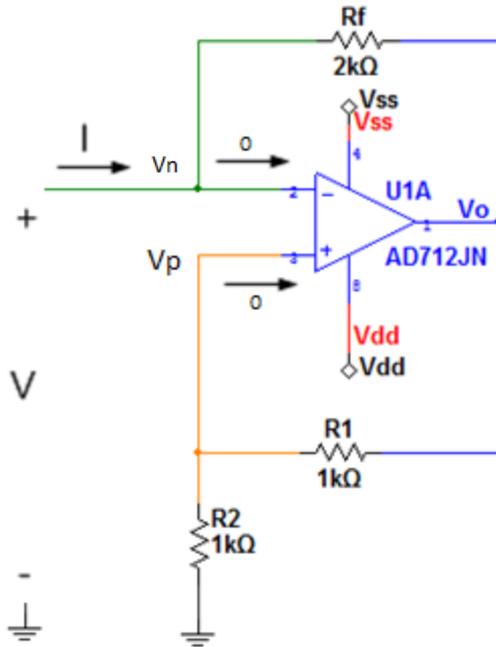


## Step 2: Devise a Plan

1. Derive i-v graph of  $N_R = I(V)$  using op-amp ideas from lecture 1
2. Use  $I = -C \frac{dV}{dt}$  (1) (concepts from circuit theory)
3. Use (1) to find and sketch  $V_o(t)$

# Step 3 (a): Carry out the plan

## 1. Terminology



## 2. Circuit Equations

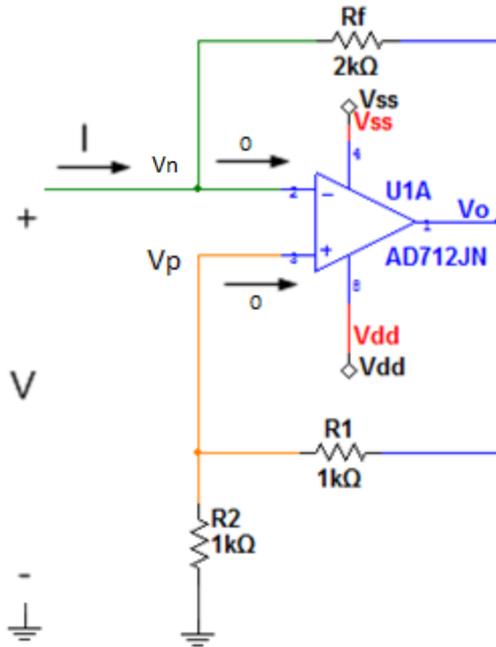
$$I = \frac{v_n - v_o}{R_f}$$
$$= \frac{V - v_o}{R_f} \quad (2)$$

$$v_p = \frac{R_2}{R_1 + R_2} v_o \quad (3)$$

3. Recall three modes of operation for an op-amp : **linear region**, **positive saturation** and **negative saturation**.

# Step 3 (b): Carry out the plan

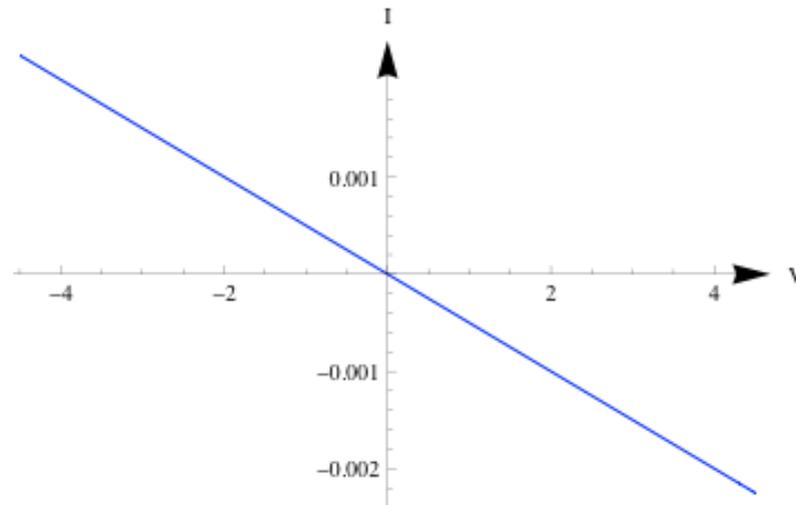
## 1. Op-amp in linear region



## 2. Circuit Equations

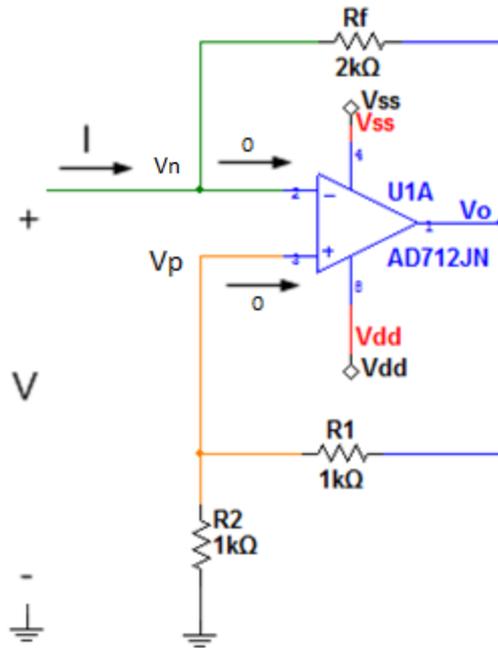
$$I = -\frac{V}{R_f} \quad (4)$$

## 3. I-V graph



# Step 3 (c): Carry out the plan

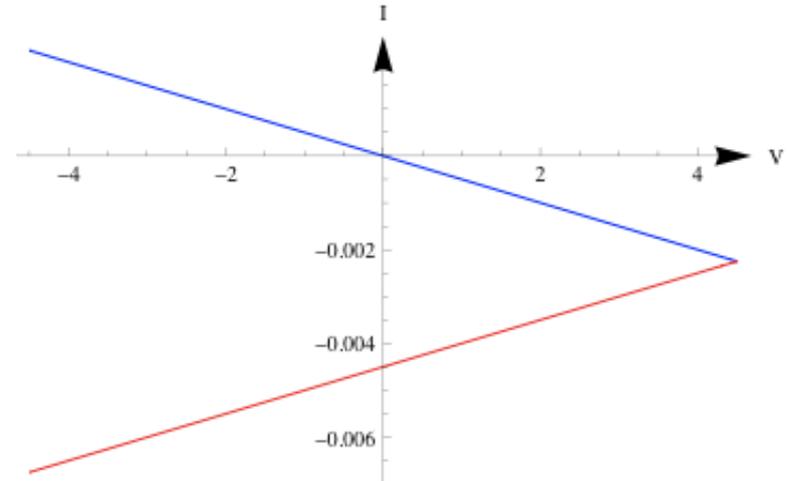
1. Op-amp in **positive saturation**



2. Circuit Equations

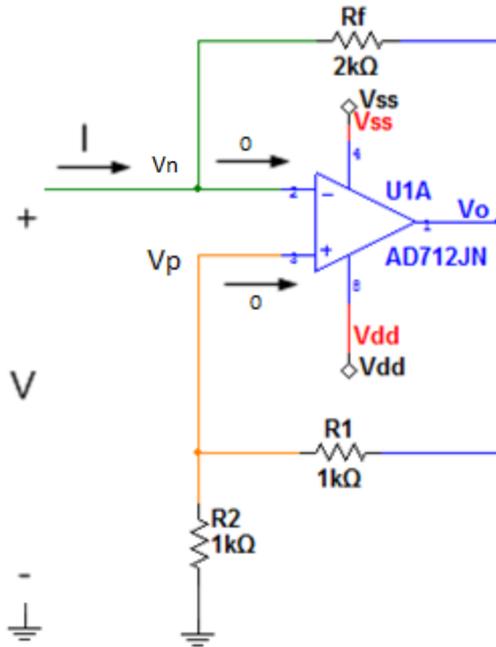
$$I = \frac{V - 9}{R_f} \quad V < 4.5 \text{ volts} \quad (5)$$

3. I-V graph



# Step 3 (d): Carry out the plan

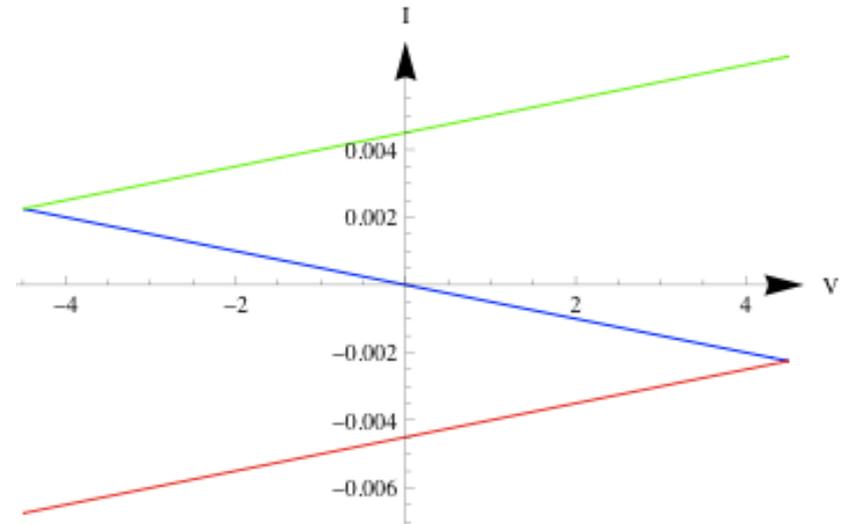
1. Op-amp in **negative saturation**



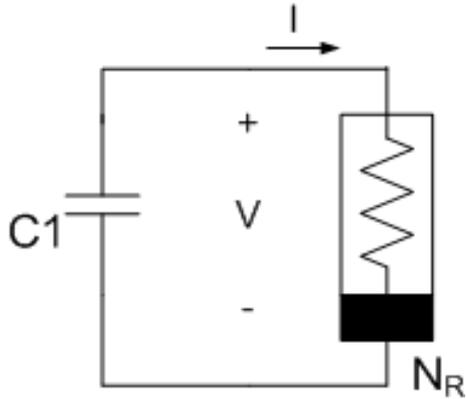
2. Circuit Equations

$$I = \frac{V + 9}{R_f} \quad V > -4.5 \text{ volts} \quad (6)$$

3. I-V graph



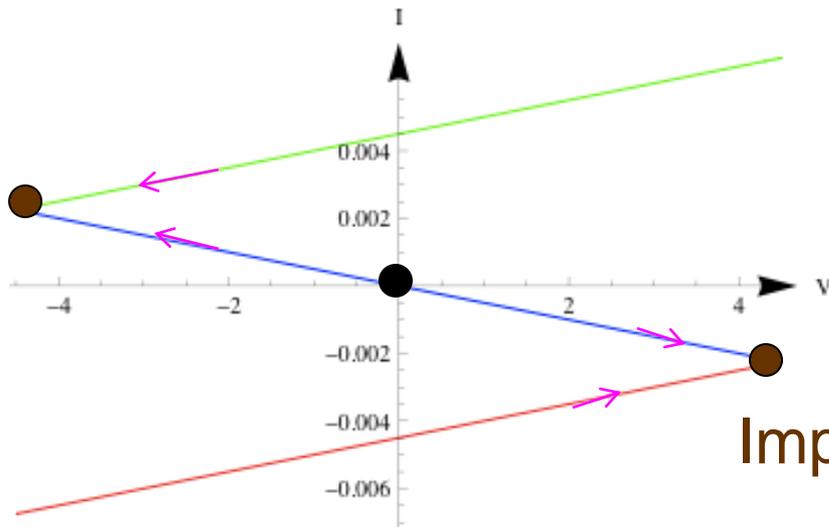
# Step 3(e) : Finding $V_o(t)$



$$I = -C \frac{dV}{dt} \quad (7)$$

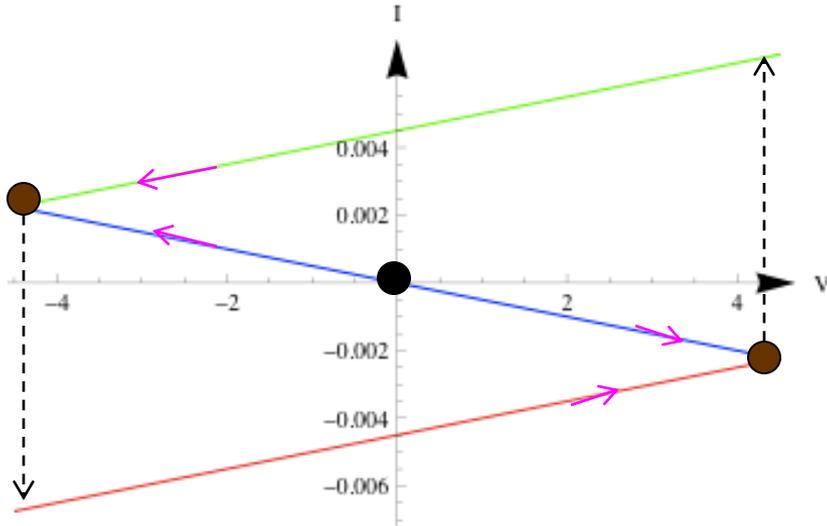
$$\text{Equilibrium points : } \frac{dV}{dt} \triangleq 0 \quad (8)$$

$$\text{Dynamic Route} \triangleq \begin{cases} I > 0 & \dot{V} < 0 \quad (C > 0) \\ I < 0 & \dot{V} > 0 \quad (C > 0) \end{cases} \quad (9)$$

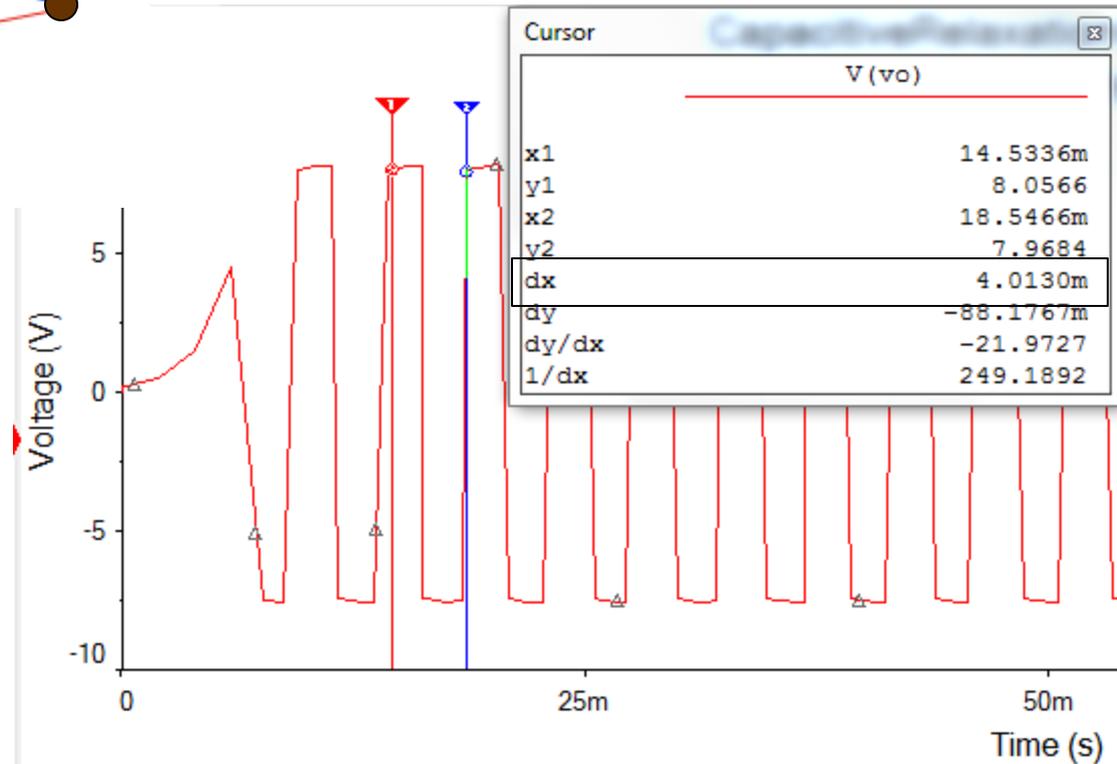


Impasse Points

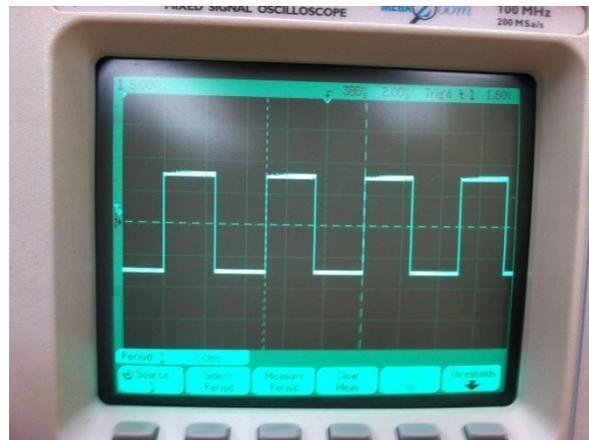
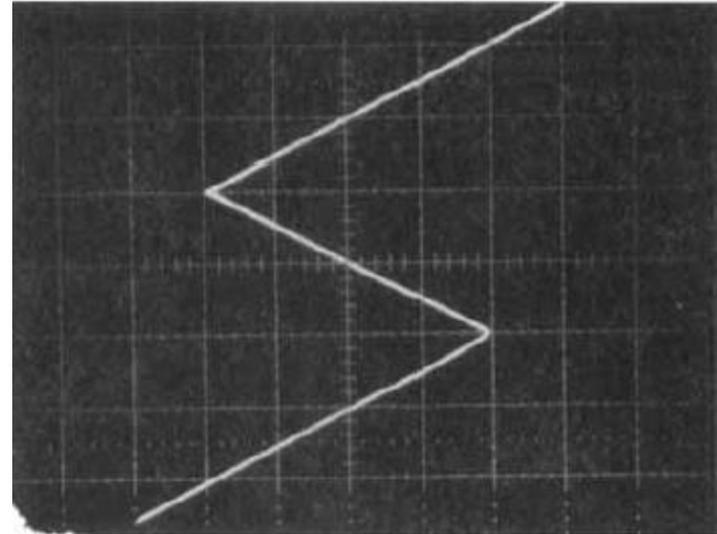
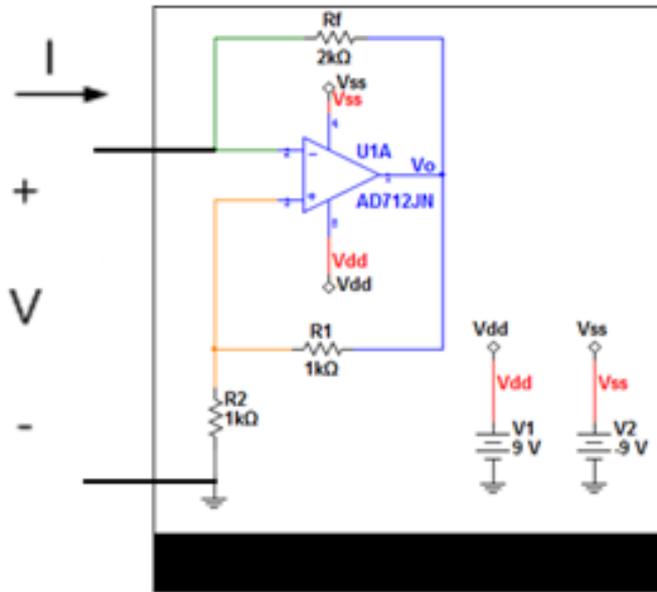
# Step 3(e) : Sketching $V_o(t)$



Period will be computed in next lecture

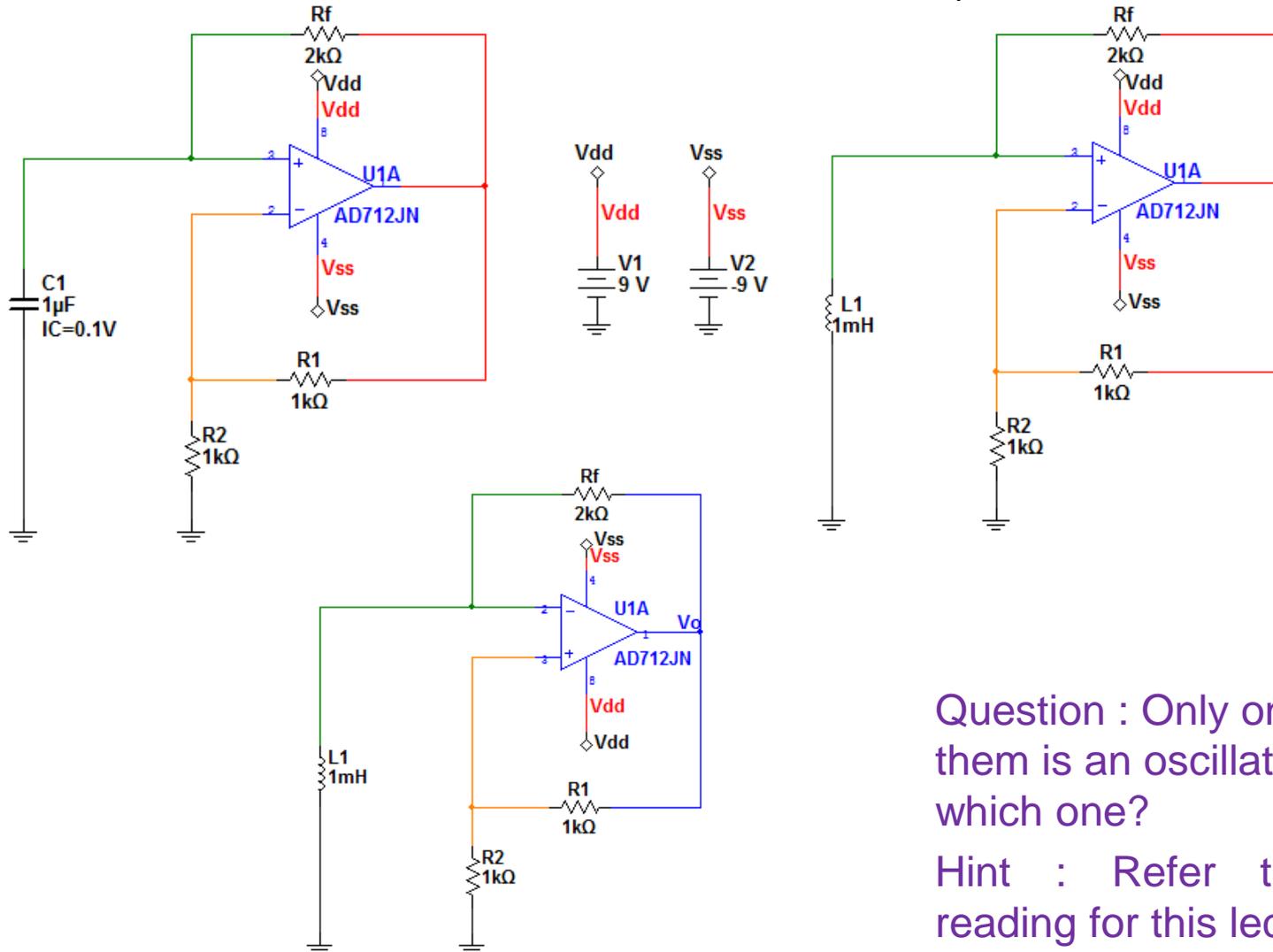


# Step 4: Check your answer



# Remember us 😊?

What does each circuit below do (answer in ONE word)?



Question : Only one of them is an oscillator, which one?

Hint : Refer to the reading for this lecture!